

#### 基于生物医学统计的信号处理

Institute of Media, Information, and Network









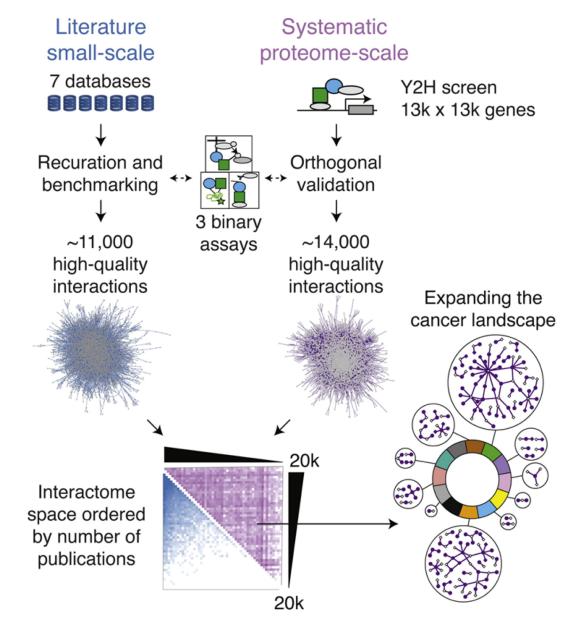
Dept. Bioinformatics& Biostatistics SJTU-Yale joint Center for Biostatistics School of Life Sciences& Biotechnology, SJTU

June 22, 2020

#### A Proteome-Scale Map of the Human Interactome Network

A systematic map of 14,000 highquality human binary proteinprotein interactions.

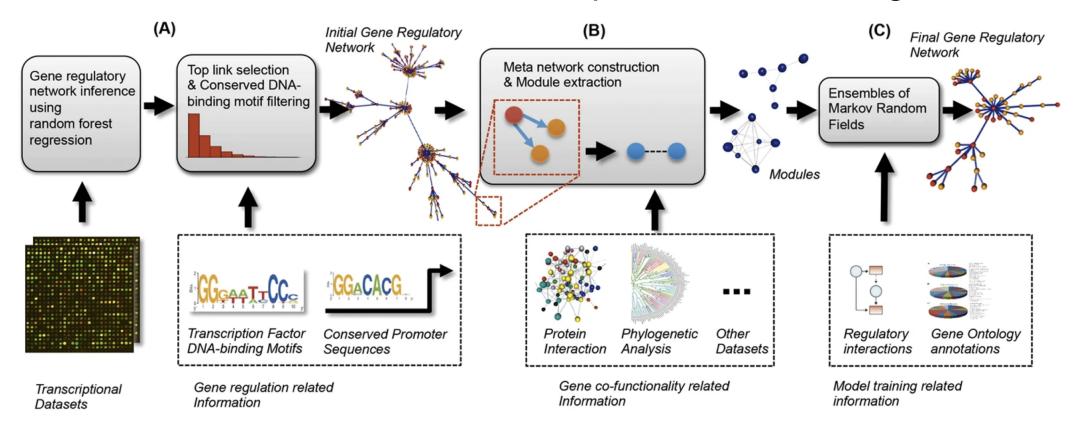
*Cell* 2014 159, 1212-1226



### Other networks

#### Regulatory network

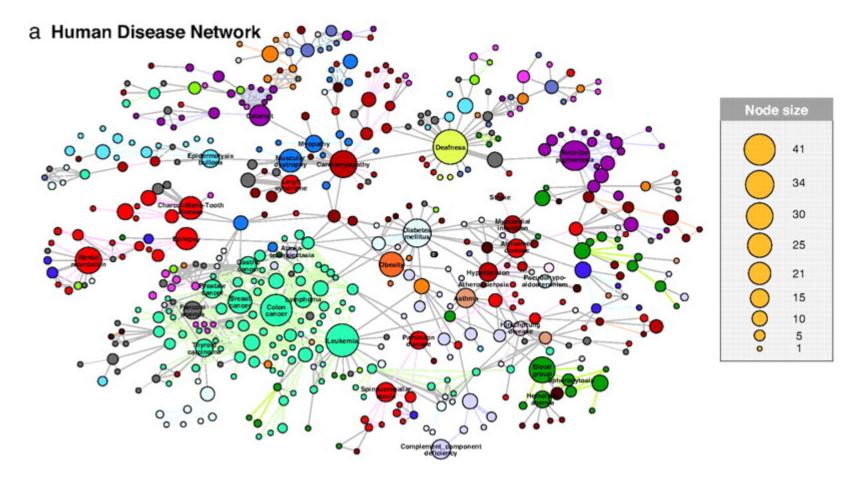
#### **Transcription factor --- Targets**



Scientific reports, 7, Article number: 41174 (2017)

### Other networks

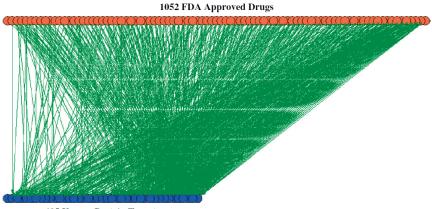
#### Disease Gene Networks



Goh et al. Proc Natl Acad Sci USA. (2007) 104:8685-90

### Other networks

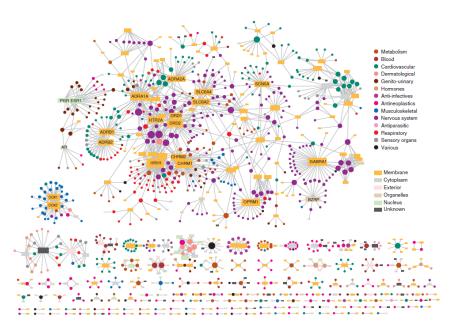
#### **Drug-Target Networks**



485 Known Protein Targets

Fig 3. Visualization of the bipartite drug-target network extracted from DrugBank. Orange nodes represent drugs and blue nodes are known biomolecular targets. The network is made of 1537 nodes (1052 drugs and 485 targets) and 1815 interactions extracted from 2240 research articles.

Ma' ayan et al. Mt Sinai J Med (2007) 74:27



Yildirim et al. Nat Biotechnol. (2007) 25:1110

### Metabolic networks

👩 KEGG: Kyoto Encyclopedia of Genes a... 🕂



» Japanese

Go

Clear

Introduction **KEGG: Kyoto Encyclopedia of Genes and Genomes** Overview Release notes A grand challenge in the post-genomic era i Current statistics **KEGG Identifiers** Pathway maps Brite hierarchies **KEGG XML KEGG API** 

**KEGG FTP** 

**KEGG Home** 

KegTools

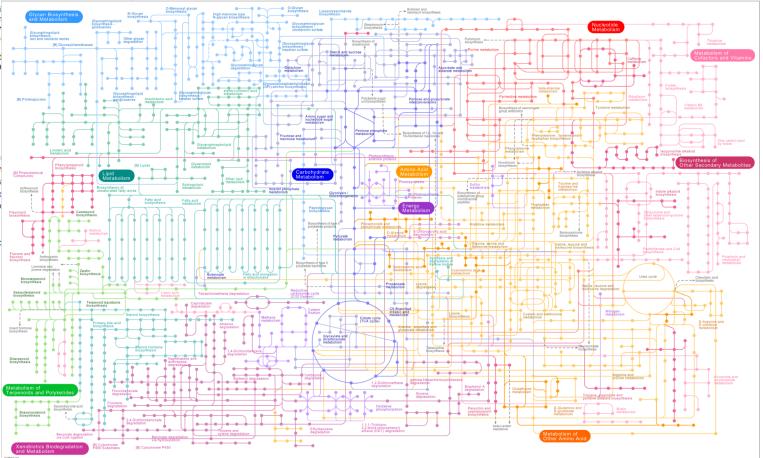
GenomeNet

DBGET/LinkDB

Feedback

representation of the cell, the organism, th biosphere, which will enable computational pr complexity of cellular processes and org genomic and molecular information. Towards developing a bioinformatics resource named research projects of the Kanehisa Laboratoric Center of Kyoto University and the Human University of Tokyo. Main entry point to the KEGG web service KEGG2 KEGG Table of Contents Data-oriented entry points KEGG PATHWAY Pathway maps and pathway Functional hierarchies and on KEGG BRITE Human diseases Disease cla KEGG DISEASE KEGG DRUG Drugs ATC drug classificatio

KEGG ORTHOLOGY KO system and ortholog anne Genes and proteins KEGG GENES KEGG GENOME Genomes KEGG organisms KEGG COMPOUND Chemical compounds Comp KEGG GLYCAN Glycans KEGG REACTION Reactions



6

# Centrality

- □ Relative **importance of a node** in the graph
- □ Which nodes are in the "center" of a graph?
  - What do you mean by "center"?
  - Definition of "center" varies by context/purpose
- "There is certainly no unanimity on exactly what centrality is or on its conceptual foundations, and there is little agreement on the proper procedure for its measurement."
  ----- by Freeman, 1979



- □ Real valued function on the nodes of a graph
- □ Structural index
- □ Applications:
  - ✓ How influential protein is in a PPI network?
  - ✓ How important a TF is?

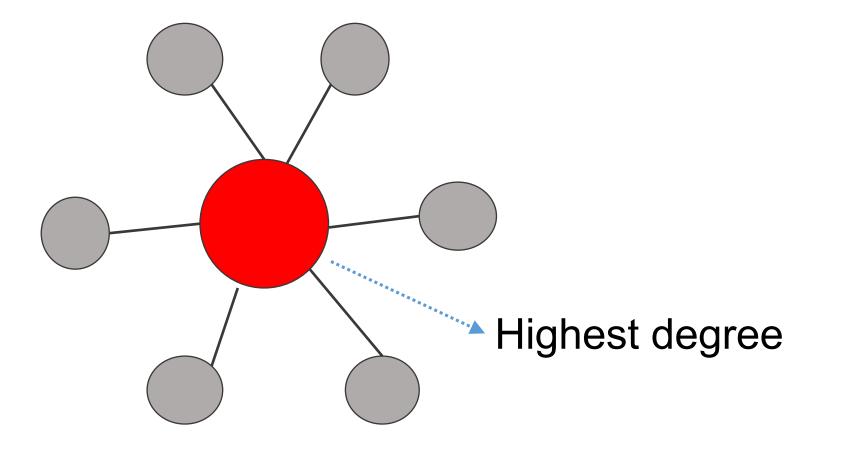
# **Centrality Measures**

- □ Degree centrality
- Betweenness centrality
- □ Closeness centrality

### Degree centrality

- Local measure of the importance of a node within a graph
- Sum of the weights of incident edges (in weighted graphs).
- Degree centrality assigns an importance score based simply on the number of links held by each node.
- Node with the highest degree is important
  - Index of exposure to what is flowing through the network
  - Hub genes
  - Gossip network: central actor more likely to hear a gossip

### Degree centrality



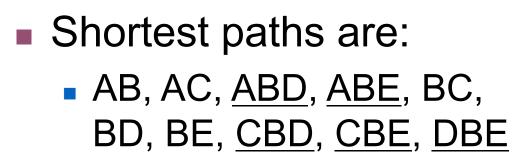
### Betweenness centrality

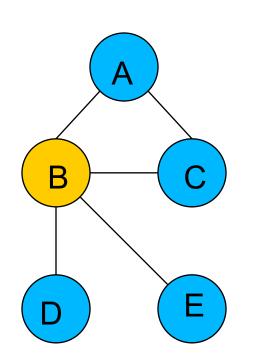
- Control on the optimal flow within a graph
- The number of shortest paths in the graph that pass through the node divided by the total number of shortest paths.

$$BC(k) = \sum_{i} \sum_{j} \frac{\rho(i,k,j)}{\rho(i,j)}, \quad i \neq j \neq k$$

where  $\rho(i, j)$  is the total number of shortest paths from node i to node j and  $\rho(i,k,j)$  is the number of those shortest paths that pass through k.

# **Betweenness centrality**





# **Betweenness centrality**

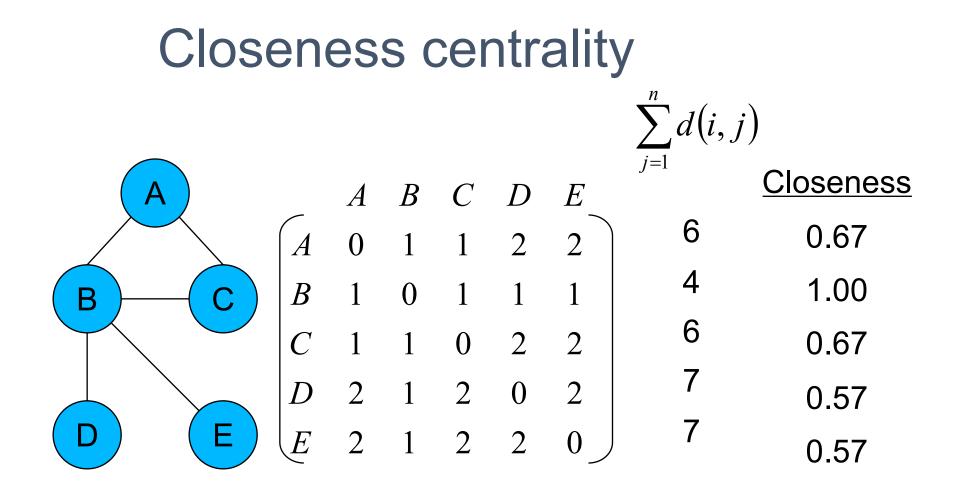
- Nodes with a high betweenness centrality are interesting because they
  - control information flow in a network
  - may be required to carry more information
- And therefore, such nodes
  - may be the subject of targeted attack

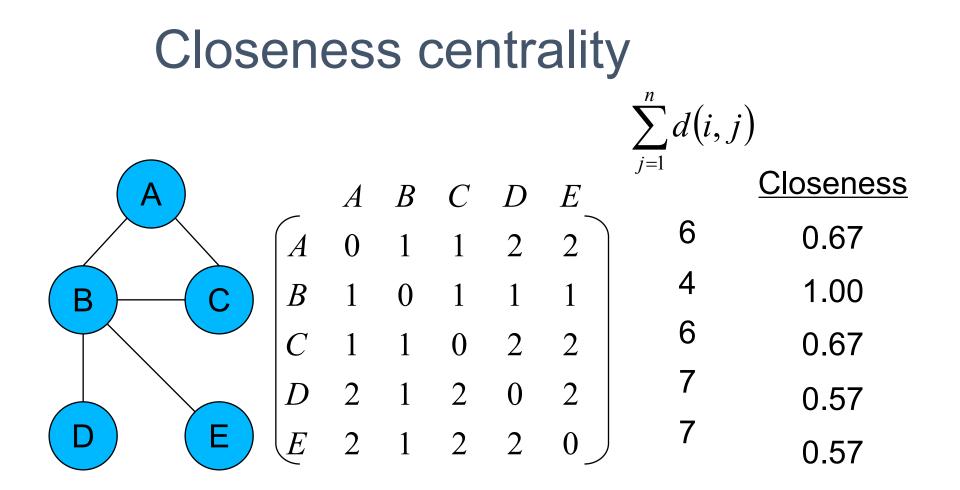
### **Closeness centrality**

- How fast information can spread from one node to every other node
- A node is considered important if it is relatively close to all other nodes.
- The normalised inverse of the sum of topological distances in the graph.

$$CC(i) = \frac{N-1}{\sum_{j} d(i, j)}$$

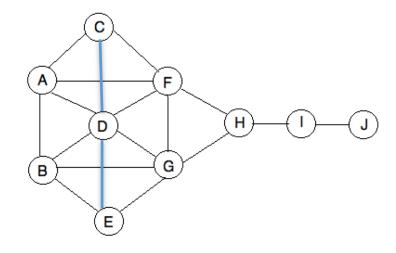
where d(i,j) is the distance (the number of edges in a shortest path) between vertices i and j.





Node B is the most central one in spreading information from it to the other nodes in the network.

• Example:



#### Which node is most important?

	Degree	Closeness	Betweeness
From highest	D	F, G	Н
	F, G	D, H	F, G
to	А, В	А, В	I
	С, Е, Н	С, Е	D
lowest		I	А, В
	J	J	C, D, J

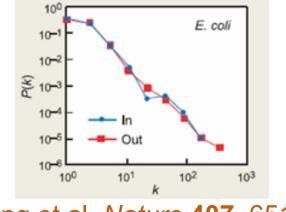
## "Real" Networks are "Scale Free"



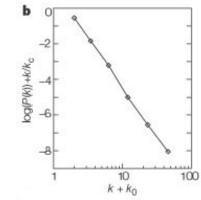
Barabasi and Albert. Science 286, 509 (1999)

Barabasi et al. found that many real networks including the Internet and the WWW are **scale-free**. This means that the connectivity distribution of nodes fits a power-law.

They analyzed databases of metabolic networks in lower organisms and the protein-protein interactions map of the yeast proteome inferred from high-throughput yeast-2-hybrid screens. All shown to have scale-free connectivity distribution.



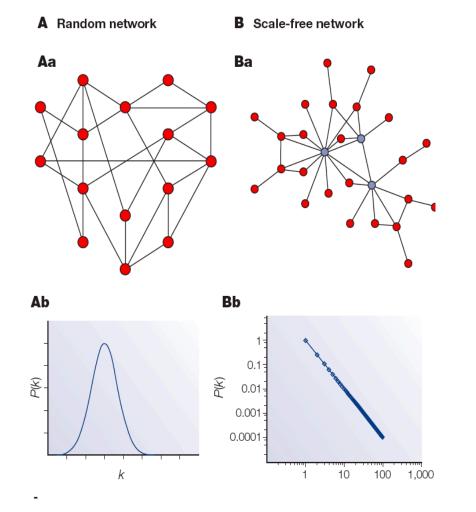
Jeong et al. *Nature* **407**, 651 (2000)



Jeong et al. *Nature* **411**, 41 (2001)

# Degree Distribution

P(k) is probability of each degree k, i.e fraction of nodes having that degree.



For random networks, P(k) is normally distributed.

For real networks the distribution is often a power-law:

 $P(k) \sim k^{-\gamma}$ 

Such networks are said to be scale-free

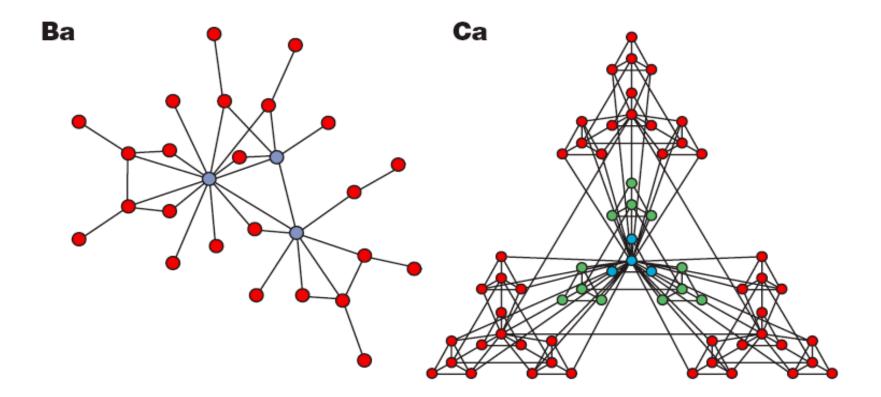
For most networks,  $2 < \gamma < 3$ 

*Nature Reviews Genetics* **5**, 101-113 (2004)

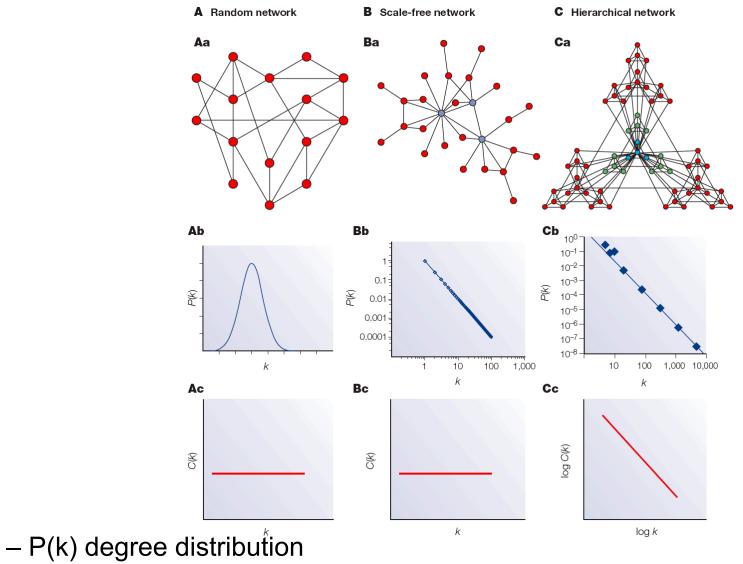
# **Hierarchical Networks**



**C** Hierarchical network



### Detecting Hierarchical Organization



- C(k) average clustering coefficient function

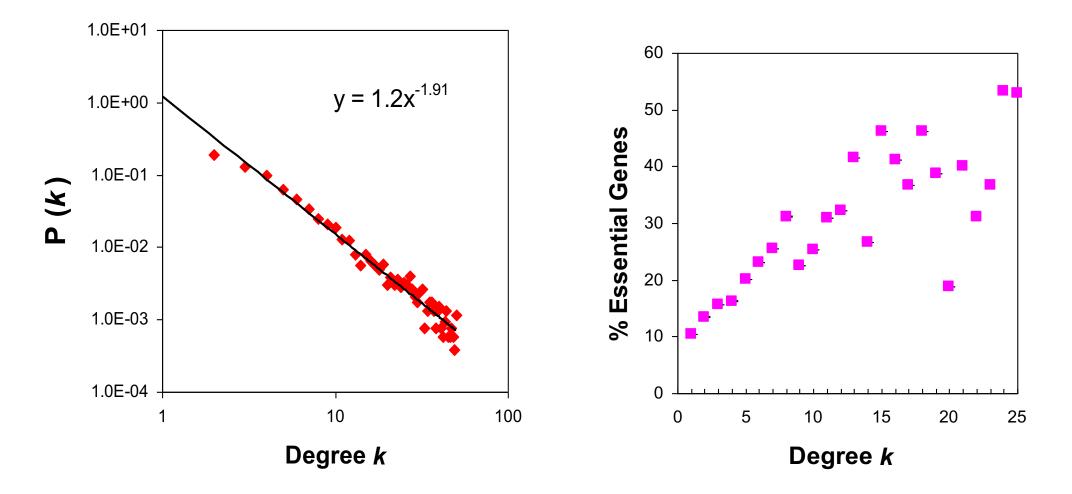
# Cellular networks are scale-free



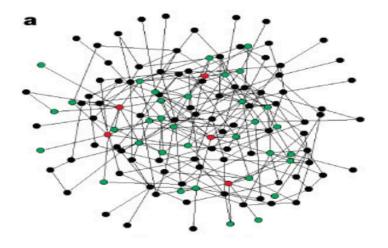
### Scale-Free Networks are Robust

- Complex systems (cell, internet, social networks), are resilient to component failure
- Network topology plays an important role in this robustness
  - Even if ~80% of nodes fail, the remaining ~20% still maintain network connectivity
- Attack vulnerability if hubs are selectively targeted
- In yeast, only ~20% of proteins are lethal when deleted, and are 5 times more likely to have degree k>15 than k<5.</li>

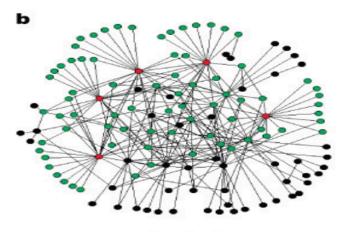
### Knock-out Lethality and Connectivity



### Random network vs scale-free network

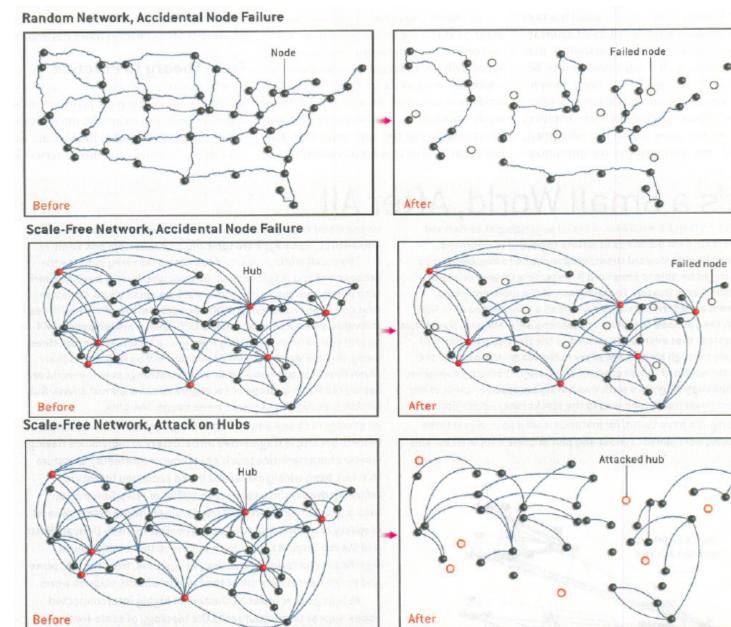


- Random network
- 130 nodes, 215 edges
- Homogeneous: most nodes have approximately the same number of links
- Five red nodes with the highest number of links reach 27% of the nodes



- Scale-free network
- 130 nodes, 215 edges
- Heterogeneous: the majority of the nodes have one or two links but a few nodes have a large number of links
- Five red nodes with the highest degrees reach 60% of the nodes (hubs)

# Degree (hubs)-attack

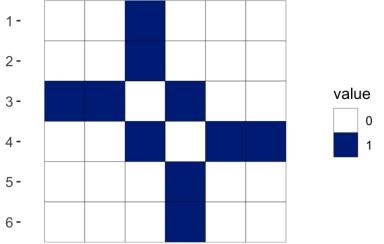


### How to encode a graph

A **graph** is formed by a set of nodes or vertices (often called VV) and a set of edges between these vertices (EE). Edges EE are provided as unordered pairs of vertices in undirected graphs and ordered pairs for directed or oriented graphs.

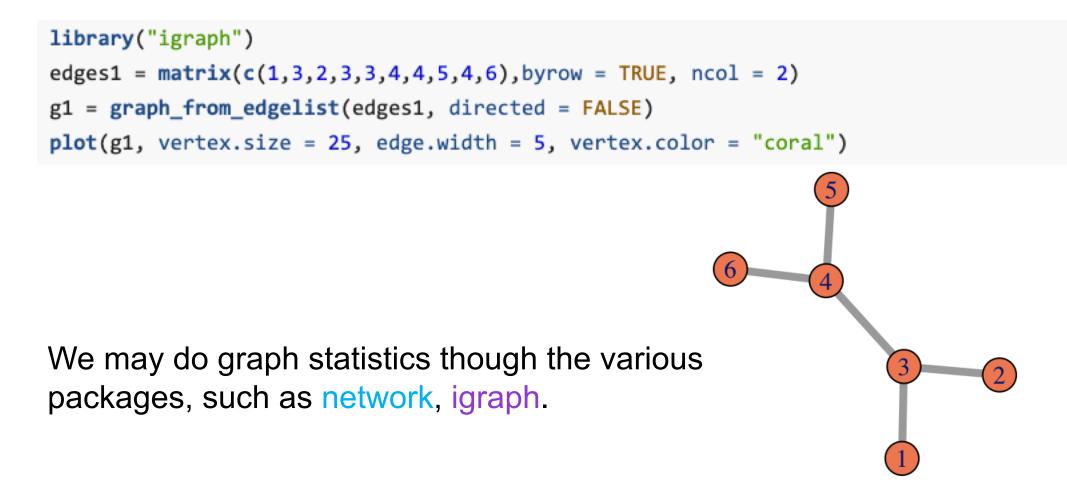
An **adjacency matrix** AA is the matrix representation of EE. AA is a square matrix with as many rows as nodes in the graph. AA contains a non zero entry in the i<sup>th</sup> row and j<sup>th</sup> column if there is an edge between the i<sup>th</sup> and j<sup>th</sup> vertices.

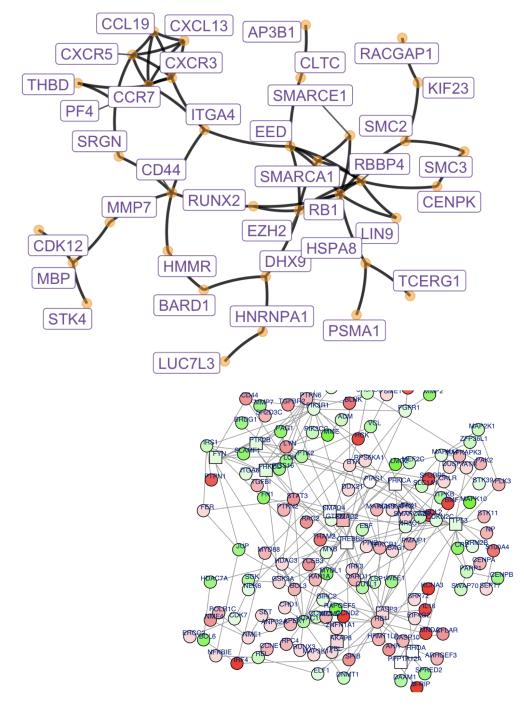
For graphs with undirected edges what is special about the adjacency matrix AA?

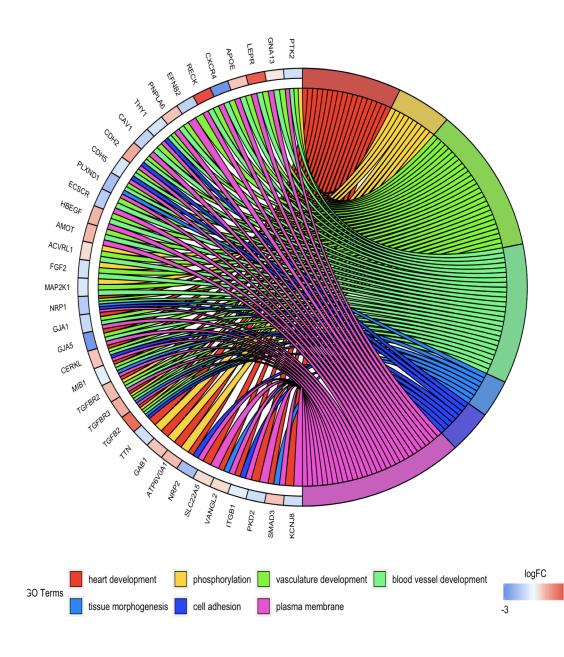


### How to encode a graph

The adjacency matrix is symmetric



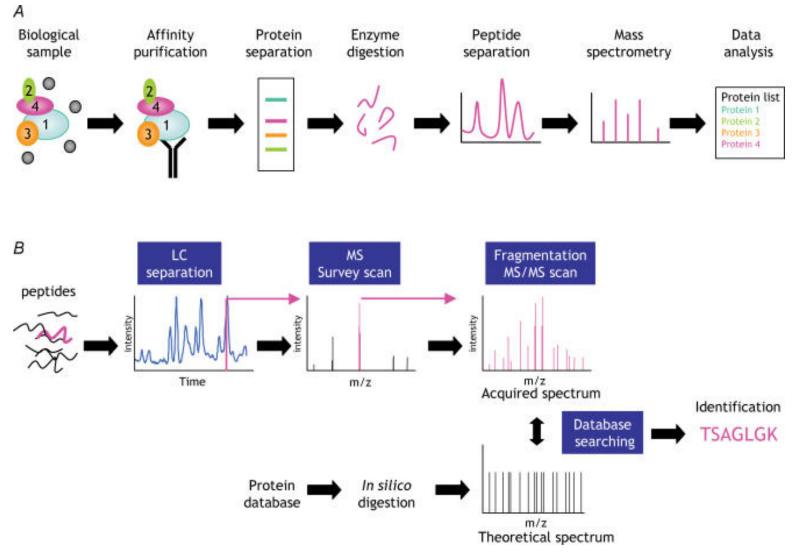




# Topics

- Network and network topology
- Network reconstruction
- Network application

### (1) Mass spectrometry screening (Pull-down)



J Physiol. 2005 February 15; 563(Pt 1): 11-21.

#### A Protein Complex Network of Drosophila melanogaster

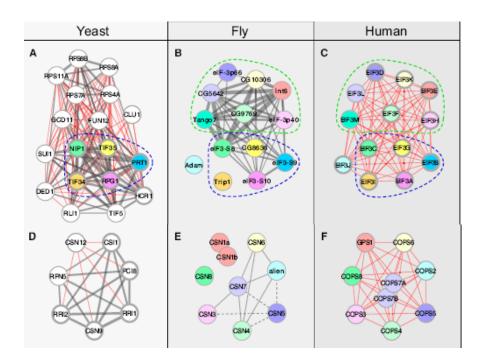
K.G. Guruharsha,<sup>1,4</sup> Jean-François Rual,<sup>1,4</sup> Bo Zhai,<sup>1,4</sup> Julian Mintseris,<sup>1,4</sup> Pujita Vaidya,<sup>1</sup> Namita Vaidya,<sup>1</sup> Chapman Beekman,<sup>1</sup> Christina Wong,<sup>1</sup> David Y. Rhee,<sup>1</sup> Odise Cenaj,<sup>1</sup> Emily McKillip,<sup>1</sup> Saumini Shah,<sup>1</sup> Mark Stapleton,<sup>2</sup> Kenneth H. Wan,<sup>2</sup> Charles Yu,<sup>2</sup> Bayan Parsa,<sup>2</sup> Joseph W. Carlson,<sup>2</sup> Xiao Chen,<sup>2</sup> Bhaveen Kapadia,<sup>2</sup> K. VijayRaghavan,<sup>3</sup> Steven P. Gygi,<sup>1</sup> Susan E. Celniker,<sup>2</sup> Robert A. Obar,<sup>1,\*</sup> and Spyros Artavanis-Tsakonas<sup>1,\*</sup>

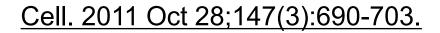
<sup>1</sup>Department of Cell Biology, Harvard Medical School, Boston, MA 02115, USA

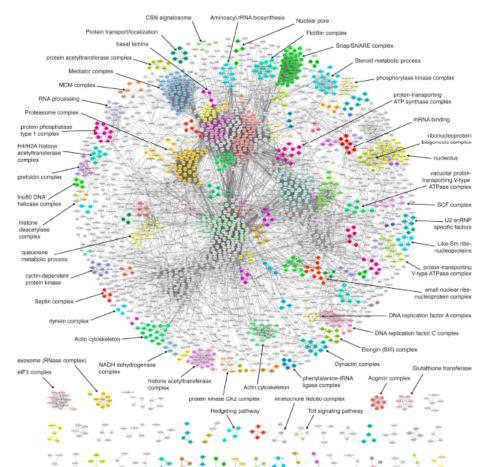
<sup>2</sup>Berkeley *Drosophila* Genome Project, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA <sup>3</sup>National Centre for Biological Sciences, Tata Institute of Fundamental Research, Bangalore 560065, India

<sup>4</sup>These authors contributed equally to this work

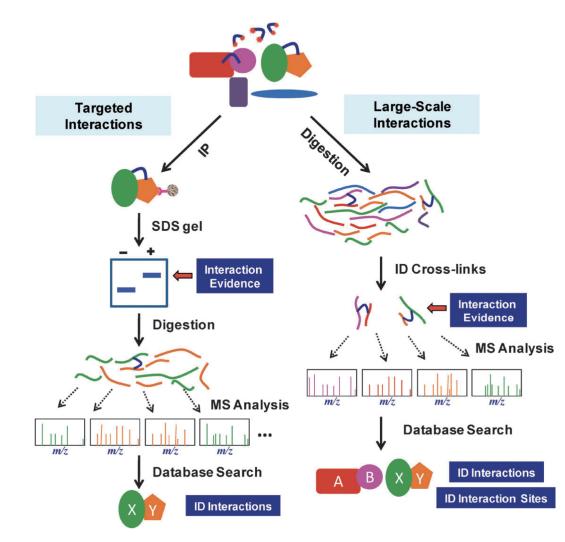
\*Correspondence: robert\_obar@hms.harvard.edu (R.A.O.), artavanis@hms.harvard.edu (S.A.-T.) DOI 10.1016/j.cell.2011.08.047







### (2) MS-based Cross-linking strategy for PPI detection



Nature Protocols 13, 2864–2889(2018)

PPI network identification

**Direct:** from an experiment

#### **Indirect: network reconstruction**

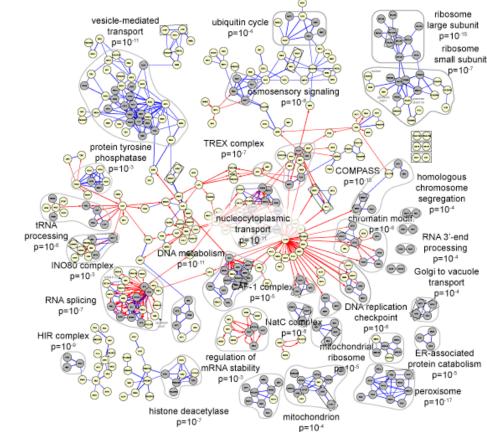
often models are needed (=

- gene co-expression
- ...., .....

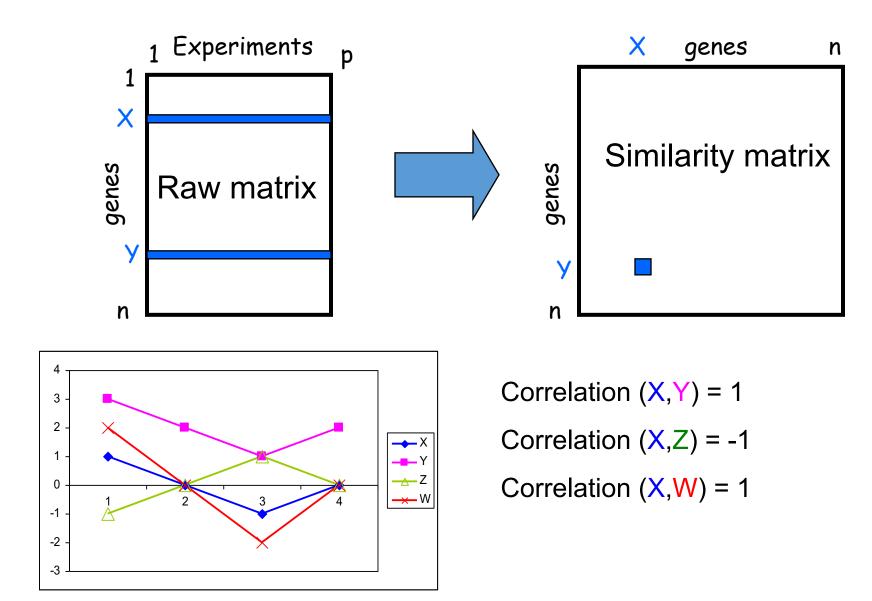
#### **Co-expression Networks**

Nodes are connected if they have a significant pairwise expression profile association across environmental perturbations

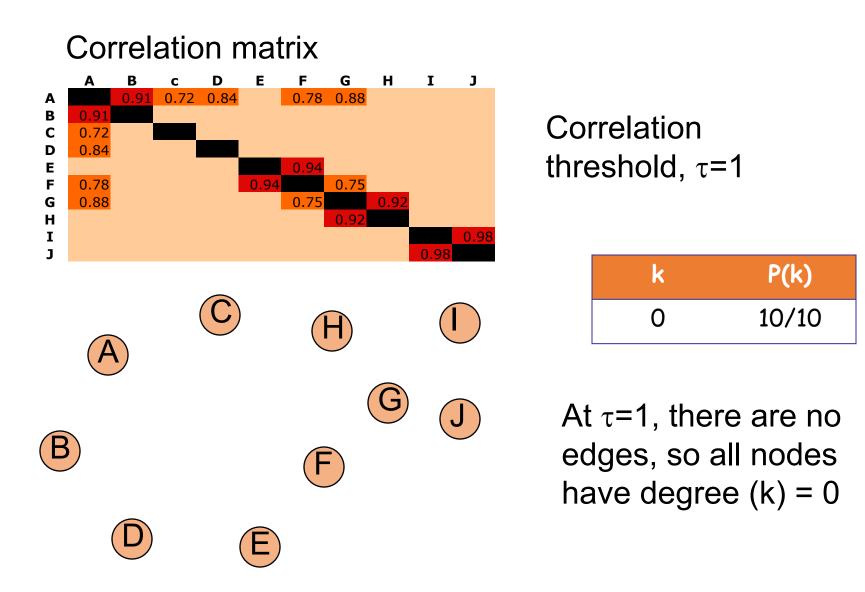
	<b>H<sub>2</sub>O<sub>2</sub></b> 0 15' 60'		<b>Cd</b> 0 15' 60'			0	Heat 0 15' 60'			<b>Sorb.</b> 0 15' 60'			<b>MMS</b> 0 15' 60'		
seue															
1682 Genes															
1															
3															
	>8x induced								>8x repressed						



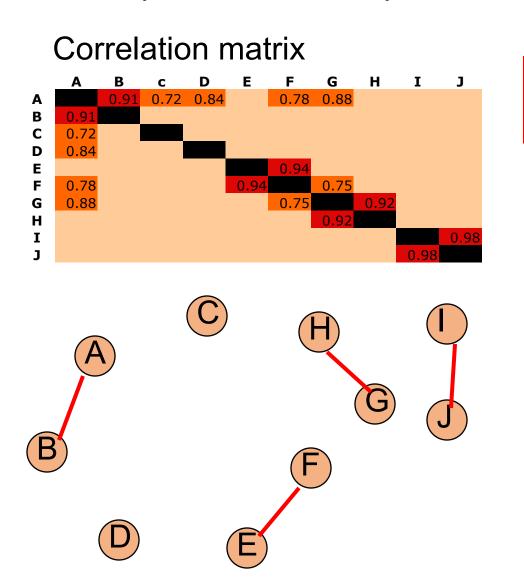
# Correlation: pairwise similarity



# Example: co-expression network



# Example: co-expression network

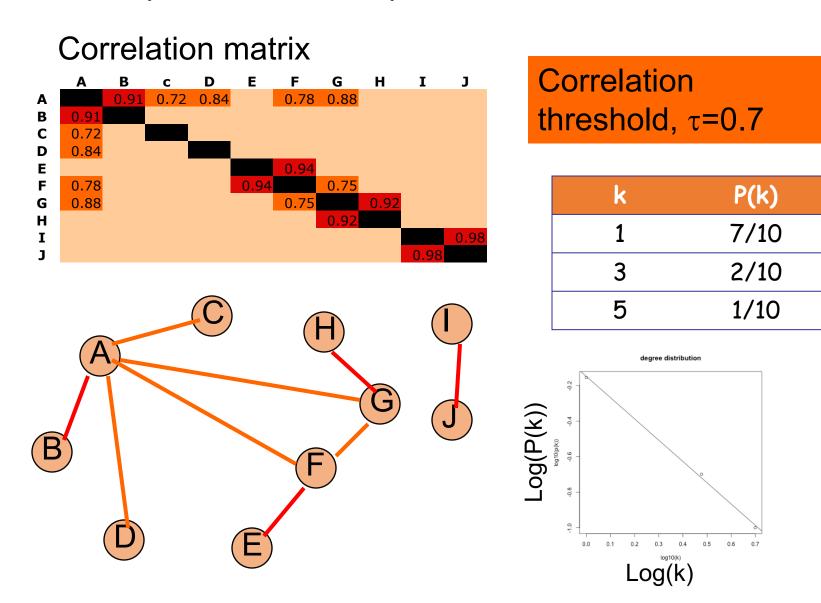


Correlation threshold, τ=0.9

k	P(k)
0	2/10
1	8/10

At  $\tau$ =0.9, there are 4 edges, so 8 nodes have degree (k) = 1

# Example: co-expression network



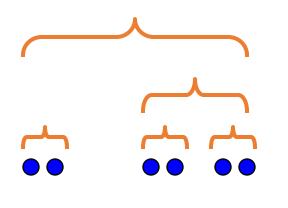
### Clustering for network reconstruction

- Clustering: extract groups of genes that are tightly coexpressed over a range of different experiments.
- Pattern discovery
- No prior knowledge required

# Clustering algorithms

- Inputs:
  - Similarity matrix
  - Number of clusters or some other parameters
- Many different classifications of clustering algorithms:
  - Hierarchical vs partitional
  - Heuristic-based vs model-based
  - Soft vs hard

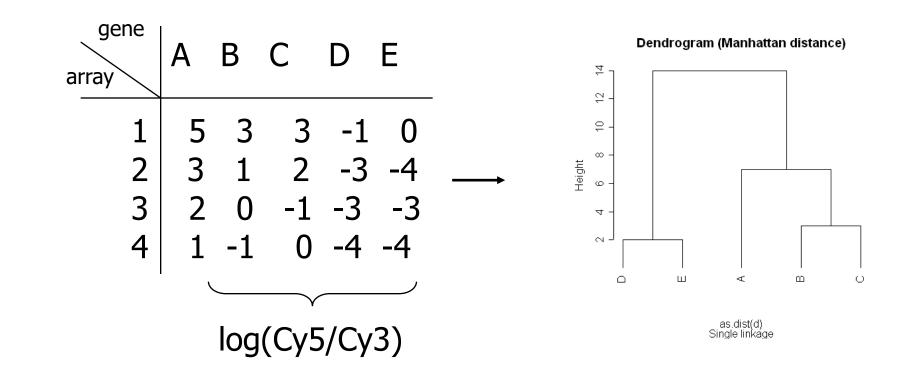
# Hierarchical Clustering



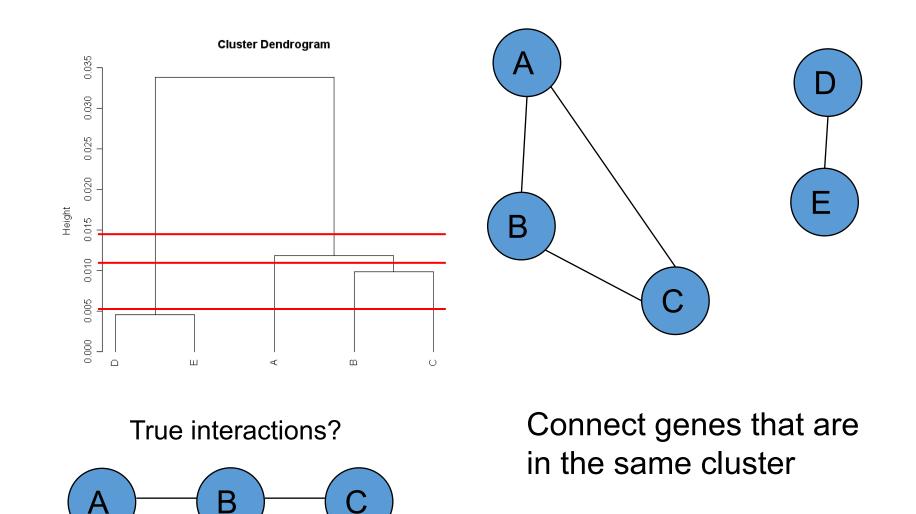
dendrogram

- Agglomerative (bottom-up)
- Algorithm:
  - Initialize: each item a cluster
  - Iterate:
    - select two most similar clusters
    - merge them
  - Halt: when required number of clusters is reached

#### **Hierarchical clustering for network reconstruction**



#### Hierarchical clustering for network reconstruction



### Weighted Co-expression Networks

- SAGMB
- WGCNA

References:

- A general framework for weighted gene co-expression network analysis (Zhang, Horvath SAGMB 2005)
- WGCNA: an R package for weighted correlation network analysis. (Langfelder, Horvath BMC Bioinformatics 2008)



# Any other type of data is helpful?

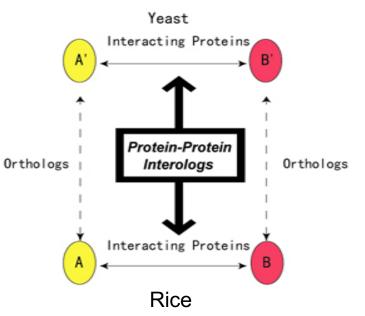


#### Interolog Mapping: Orthologs

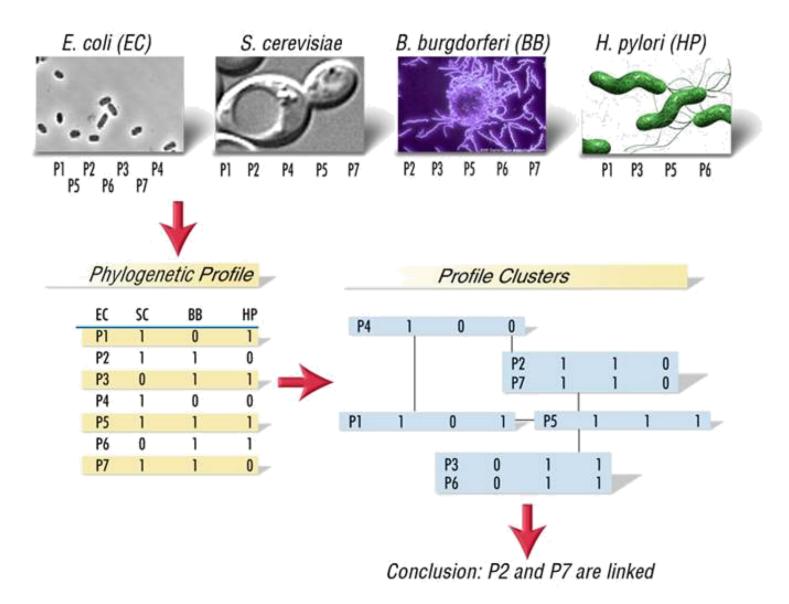
#### Interest in Orthologs

#### Maintain function $\rightarrow$ Maintain interactions

- Key concept: If A and B interact in one spe orthologs A' and B' will interact
- (A' & B') = "interologs" of (A & B)
- Defining Orthologs
  - Loose definition: Top-blast hit
  - Stringent definition: Reciprocal top-blast hit
  - Not all orthologs can be found using above definitions

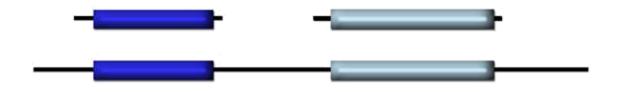


Gu et al (2011) PRIN: a predicted rice interactome network. BMC Bioinformatics.12:161, STRING Network



Pellegrini M, Marcotte EM, Thompson MJ, Eisenberg D, Yeates TO, Assigning protein functions by comparative genome analysis: protein phylogenetic profiles. Proc Natl Acad Sci U S A. 96(8):4285–8, 1999

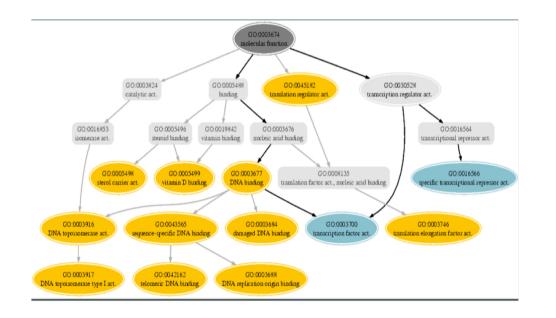
#### **Protein Fusions**



#### Monomeric proteins that are found fused in another organism are likely to be functionally related and physically interacting.

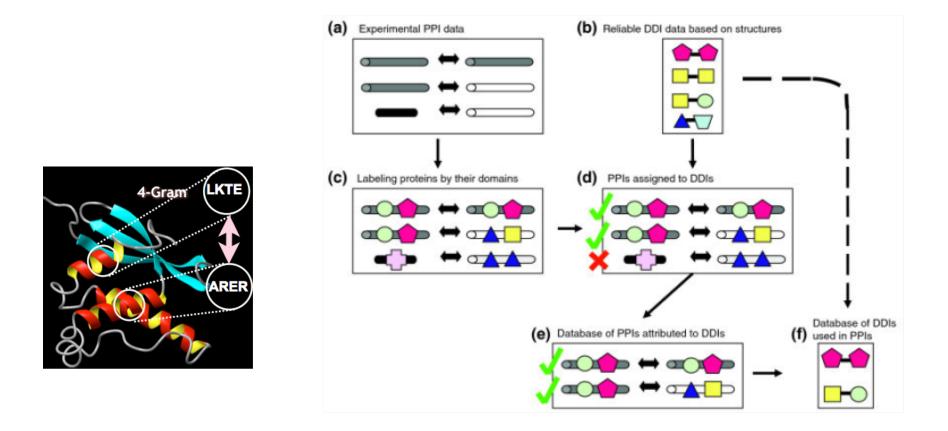
Marcotte EM, Pellegrini M, Ng HL, Rice DW, Yeates TO, Eisenberg D, Detecting protein function and protein-protein interactions from genome sequences. *Science* 285(5428):751-3, 1999

#### GO similarity (gene function)



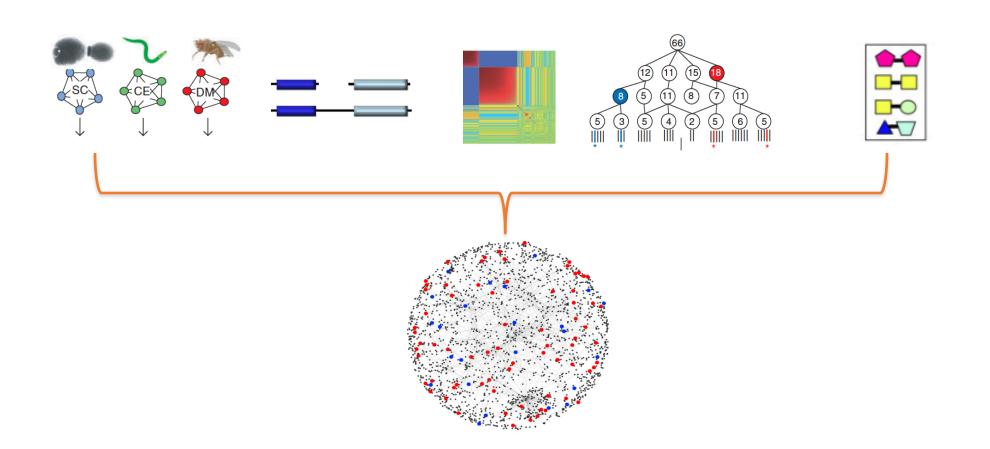
Proteins with the same biological function are more likely to physically interact than those without. In addition, proteins sharing a more specific annotation are more likely to interact than those sharing a commoner less specific annotation.

#### Interaction Domain(DDI)



Zhang et al, GAIA: a gram-based interaction analysis tool – an approach for identifying interacting domains in yeast. BMC Bioinformatics 2009, 10(Suppl 1):S60

### Integrating data



### Integrating experimental data

- Instead of using only one type of data use several types.
- This will:
  - give more supporting evidence that a protein performs a certain function.
  - reduce the number of false positive and false negative interactions.
  - give a more complete picture of the interactions between different elements involved in a certain biological process.

Probabilistic network approach

**Bayesian Approach** 

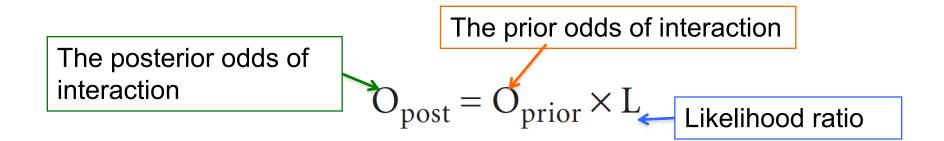
Each "interaction" link between two proteins has a posterior probability of existence, based on the quality of supporting evidence.

Rhodes et al (2005). Nature Biotechnology 23(8):951-9.

### Bayesian Approach

- A scalar score for a pair of genes is computed separately for each information source.
- Using gold positives (known interacting pairs) and gold negatives (known non-interacting pairs) interaction likelihoods for each information source is computed.
- The product of likelihoods can be used to combine multiple information sources
  - Assumption: A score from a source is independent from a score from another source.

### Bayesian Approach for PPI Prediction



$$L = Pr(f_1...f_n \mid GSP) \div Pr(f_1...f_n \mid GSN)$$

$$L = \prod_{i=1}^{i=n} \Pr(f_i \mid GSP) \div \Pr(f_i \mid GSN)$$

Constant value  $O_{\text{prior}} = P(\text{pos}) / P(\text{neg})$ ,

### Computing the likelihoods

- <u>Partition</u> the pair scores of an information source into bins and provide likelihoods for score-ranges
- E.g. Using the microarray information source and using Pearson correlation for scoring protein pairs you may get scores between -1 and 1. You want to know what is the likelihood of interaction for a protein pair that gets a Pearson correlation of 0.9.

# Partitioning the scores

pearson corr.	Likelihood (L)
(0.8,1.0]	
(0.6,0.8]	
(0.4,0.6]	
(0.2,0.4]	
(0.0,0.2]	
(-0.2,0.0]	
(-0.4,-0.2]	
(-0.6,-0.4]	
(-0.8,-0.6]	
[-1.0,-0.8]	

# Computing the likelihood

• P(Interaction | Score) / P (Interaction)

| = -----

P(~Interaction | Score) / P (~Interaction)

 $Pr(f_i | GSP) \div Pr(f_i | GSN)$ 

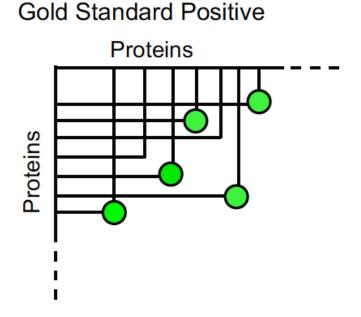
#### Example:

# Partitioning the scores

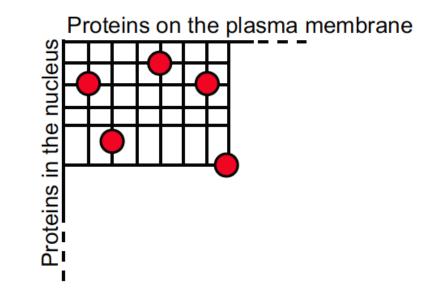
pearson corr.	P(exp pos)	P(exp neg)	Likelihood (L)
(0.8,1.0]	0.4	0.05	0.4/0.05=8
(0.6,0.8]			
(0.4,0.6]			
(0.2,0.4]	0.15	0.12	0.15/0.12=1.25
(0.0,0.2]			
(-0.2,0.0]			
(-0.4,-0.2]			
(-0.6,-0.4]			
(-0.8,-0.6]			
[-1.0,-0.8]			

### Training data sets

A Bayesian networks approach for predicting PPI



Gold Standard Negative



von Mering, et al Nucleic Acids Res. 2005

### Example

 A Bayesian networks approach for predicting protein-protein interactions from genomic data

Data type	Dataset		# protein pairs	Used for	
	In-vivo pull-	Gavin et al.		31,304	Integration of
Experimental interaction	down	Ho et al.		25,333	experimental
data	Yeast two-	Uetz et al.		981	interaction
uala	hybrid	lto et al.		4,393	data (PIE)
	Everagion	Rosetta compendium		19,334,806	
Other	Expression	Cell cycle		17,467,005	De novo
genomic	Biological	GO biological process			prediction
features	function	MIPS function		6,161,805	(PIP)
	Essentiality			8,130,528	
Gold standards	Positives	Proteins in the same MIPS complex		8,250	Training &
	Negatives	Proteins separated by localization		2,708,746	testing

Jansen et al. (2003) Science.

# Some data ... ...

	Expression correlation	# protoin poirc	Gold standard overlap				L
Expression correlation		# protein pairs	pos	neg	P(exp pos)	P(exp neg)	L
	0.9	617	16	45	2.10E-03	1.68E-05	124.93
	0.8	4,127	137	563	1.80E-02	2.10E-04	85.50
	0.7	14,979	530	2,117	6.96E-02	7.91E-04	87.97
	0.6	36,145	1,073	5,597	1.41E-01	2.09E-03	67.36
	0.5	81,102	1,089	14,459	1.43E-01	5.40E-03	26.46
	0.4	189,369	993	35,350	1.30E-01	1.32E-02	9.87
	0.3	444,757	1,028	83,483	1.35E-01	3.12E-02	4.33
	0.2	1,016,105	870	183,356	1.14E-01	6.85E-02	1.67
Se	0.1	2,205,895	739	368,469	9.71E-02	1.38E-01	0.70
Values	0	8,118,256	894	1,244,477	1.17E-01	4.65E-01	0.25
Š	-0.1	2,345,009	164	408,562	2.15E-02	1.53E-01	0.14
	-0.2	1,038,181	63	203,663	8.27E-03	7.61E-02	0.11
	-0.3	399,554	13	84,957	1.71E-03	3.18E-02	0.05
	-0.4	131,361	3	28,870	3.94E-04	1.08E-02	0.04
	-0.5	40,759	2	8,091	2.63E-04	3.02E-03	0.09
	-0.6	15,289	-	2,134	0.00E+00	7.98E-04	0.00
	-0.7	6,795	-	807	0.00E+00	3.02E-04	0.00
	-0.8	1,886	-	261	0.00E+00	9.76E-05	0.00
	-0.9	55	-	12	0.00E+00	4.49E-06	0.00
	Sum	16,090,241	7,614	2,675,273	1.00E+00	1.00E+00	1.00

### Some data ....

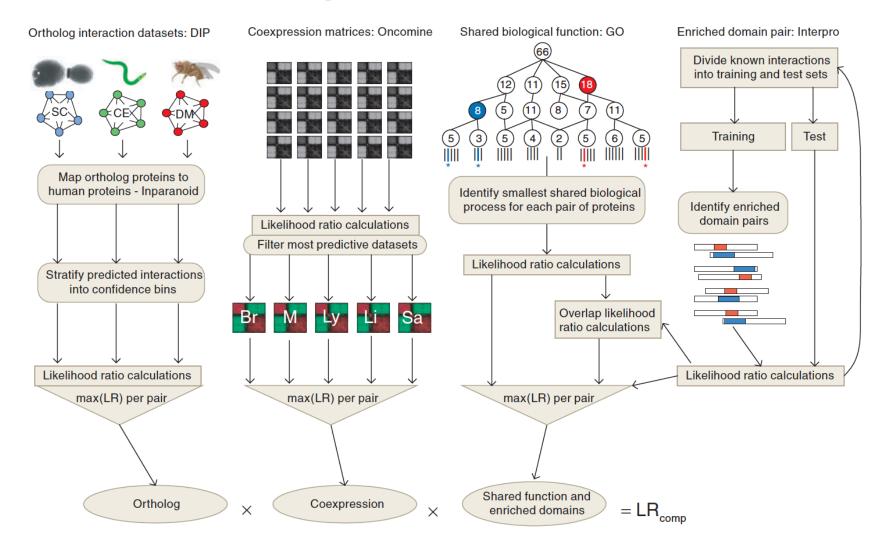
Essentiality		# protein pairs	Gold-standard overlap		P(Ess pos) P(Ess neg)	,	
	Essentiality	# protein pairs	pos	neg	r(Essipus)	r(Essineg)	L
es	EE	301,088	1,114	81,924	5.18E-01	1.43E-01	3.63
alue	NE	2,481,701	624	285,487	2.90E-01	4.98E-01	0.58
< S	NN	4,771,865	412	206,313	1.92E-01	3.60E-01	0.53
	Sum	7,554,654	2,150	573,724	1.00E+00	1.00E+00	1.00

GO biological process similarity		# protein pairs	Gold stand	old standard overlap		P(GO neg)	1
60 1	nological process similarity	# protein pairs	pos	neg	P(GO pos)	F(GOIneg)	2
	1 – 9	4,789	88	819	1.17E-02	1.27E-03	9.22
es	10 99	20,467	555	3,315	7.38E-02	5.14E-03	14.36
alue	100 – 1000	58,738	523	10,232	6.95E-02	1.59E-02	4.38
2	1000 10000	152,850	1,003	28,225	1.33E-01	4.38E-02	3.05
	10000 – Inf	2,909,442	5,351	602,434	7.12E-01	9.34E-01	0.76
	Sum	3,146,286	7,520	645,025	1.00E+00	1.00E+00	1.00

If we set  $L_{cut}$ =600, given protein A and B, their expression correlation=0.85, GO similarity=156, Essentiality value=EE, is there interaction between them?

#### L=85.50\*3.63\*4.38=1359.40 > 600

# More examples



Rhodes, et al. Probabilistic model for the human protein-protein interaction network, Nature Biotechnology (2005)

# Topics

- Network and network topology
- Network reconstruction
- Network application

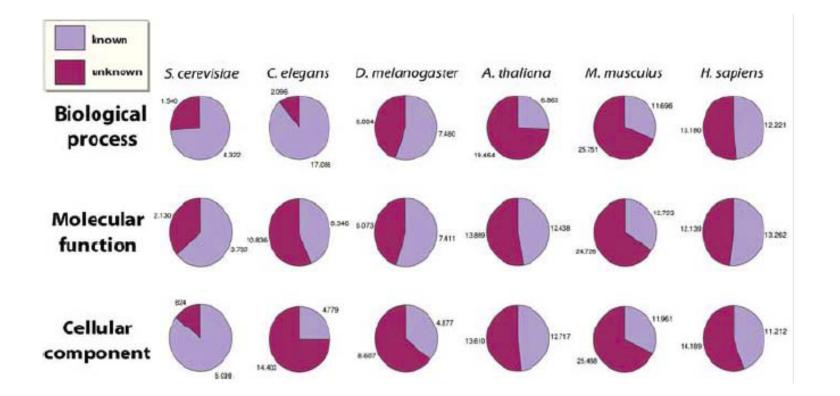
### Network application in biomedicine

Gene/Protein functional annotation

Key/disease gene prioritization

Network-based biomarker or molecular signature

### Protein function prediction



What can we do with these molecular networks? Using the position in networks to describe function

Contractor

Antoin 'Tony

Rezko

Campaign

fundraise

STATE HEALTH AND PENSION BOARDS

Stuart

Levine

Board

Illinois

Health

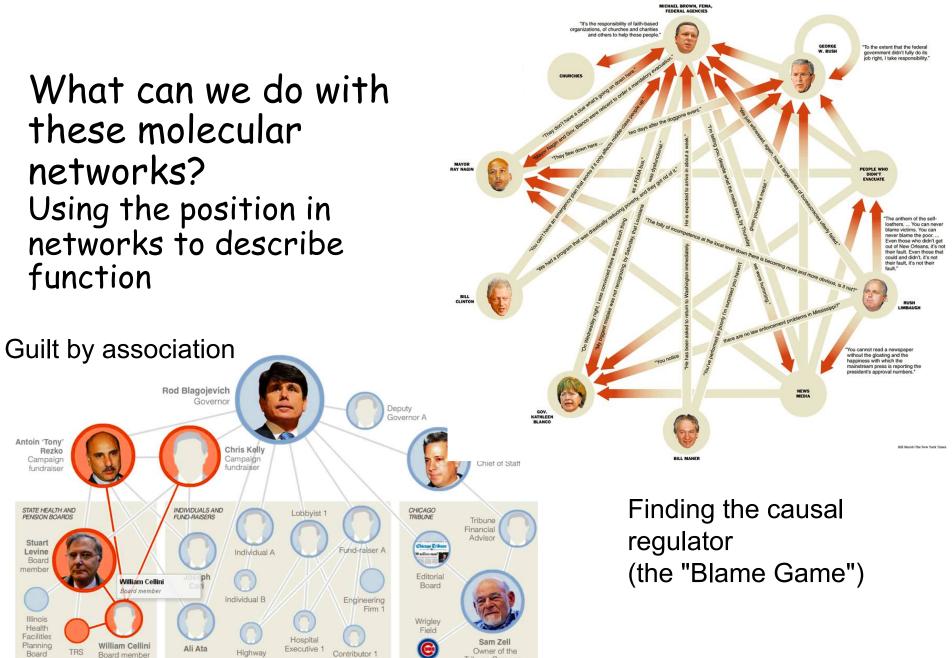
Facilities

Planning

Board

TRS

membe

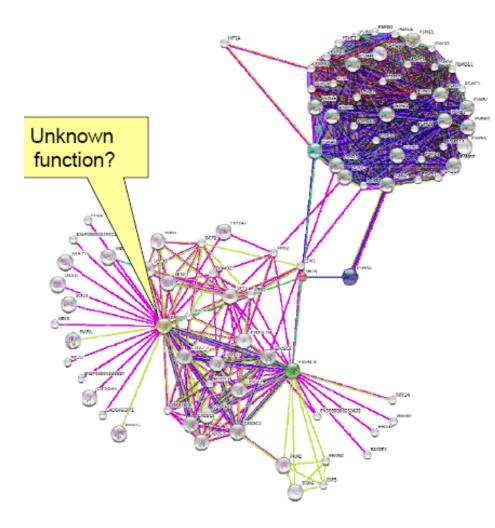


Tribune Company

70

Courtesy of Mark Gerstein

## Protein function prediction



#### Majority voting (Local)

#### K-neighborhood

-Generalized majority voting

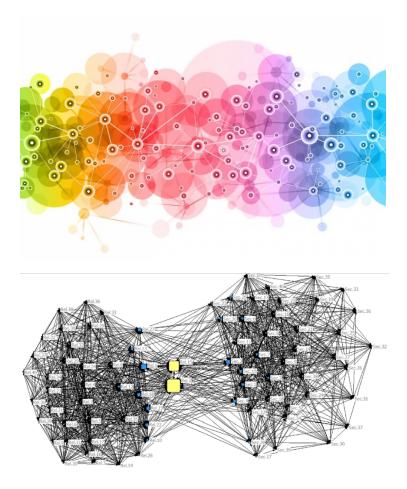
#### Chi square

- Functional enrichment among the kneighborhood as measured by the chi square score

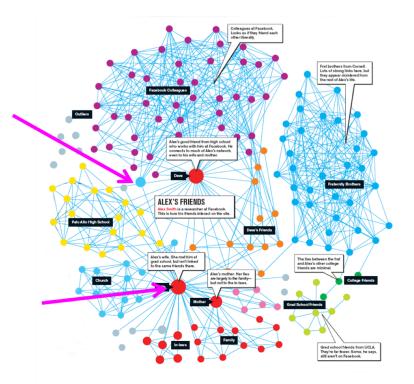
#### Module-assisted

- Module identification
- Functional enrichment evaluation

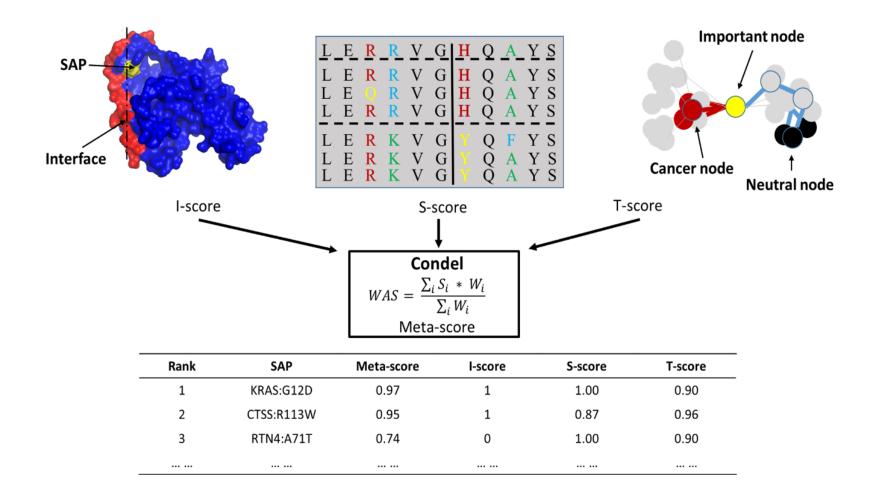
### Key/disease gene prioritization



### Degree ? Betweenness ?



#### **Network-based risk evaluation for SAPs in cancer**



# **Big Challenges**

- Strategies for explaining unmatched spectrum (30%-50%)
- How to refine genome annotation using proteome and transcriptome data
- How to do protein identification when the reference genome is unknown
- Omics integration and clinical application
- Single cell , meta-omics, pan-omics, phen-omics ?

#### Institute of Media, Information, and Network





Thanks